|                  | No: 123AN  |   | x x + +   | #4X4 Xh<br>X 4<br>*4X4 XXX.<br>1 7 1   | **** ****  | R15  | <br>  |     |
|------------------|--|---|---|--|--|--|---|-----|
| J                | AWAHAR<br>B.Tech   | II Year I Se  | U TECHNOLO<br>mester Examin<br>OBABILITY A  | ations, Novem  | ber/December   | DERABAD<br>r - 2016  | ,   | *** |
|                  |  | (Common   | to ME, CSE, IT,   | MCT. AME. V  | ILS<br>IIE MSNT)                                       |  |   |     |
| Time:            | 3 Hours  |   |   |  |  | Max. Marks:  | 75  | **  |
| Note:            | Part A is constant B c | ompulsory with onsists of 5 ion carries 10  | tains two parts thich carries 25 re<br>Units. Answer                              | marks. Answer<br>er any one fi<br>y have a, b, c as                          | all questions in<br>all question f<br>s sub questions. | n Part A.<br>From each u   | nit.  |     |
| }` }             | .:   |   | PAR   | T- A   |  |  |   | ř   |
| b)<br>d)<br>e) ] | Prove that the Prove that coefficients Define councorrelated Define Type A sample co. 2.25. Is it results to the Provention of the Provent | the total area<br>coirclation<br>variance of<br>d.<br>e-I and Type-<br>of size 10 dra<br>casonable to a | wn from a nor<br>assume that the  | al curve is unity the geometric ariables. When mal population mean of the po | mean of the are two rains has a mean 3 pulation is 30° | two regressing two regressing two materials and variance of the control of the co | ree [2] [3] [5] [6] [2] [8] [8] [8] [8] [8] [8] |     |
| h) E i) V j)I    | Explain the<br>Write down  | operating cha<br>the Chapman  | steady state in<br>racteristics of a<br>-Kolmogorov e<br>;: ;<br>ry matrix of a M | queueing syste<br>quations.  | m.   |  | 8]<br>2]<br>te                                  |     |
| ų.               | istilodtion.   |   | PART  | -B   |  | [3   | ]   |     |
| b) E             | ma ine prot  | oability mass<br>omial distribu   | fined as the surfunction of X artion. Derive its                                  | n on the faces will the expected   | value of X.  |  | d   |     |
| 68 68            | ipiain norr<br>.22 inches  | nal distribut<br>with a vari  | ctation. Prove the ion. If the mance of 10.8 is expect to have 6                  | ean height of<br>nches, how m  | sorghum va   | rieties to:b   | f ·   |     |
| ****             | ::<br>:  | Ë   |   | FG   |  | FĠ   |   |     |

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| 4.a)Obtain the rank-correlation coefficient for the following data:  | **** ****<br>**** **** |
|--|------------------------|
| X     68     64     75     50     64     80     75     40     55     64       Y     62     58     68     45     81     60     68     48     50     70  |                        |
| b) The joint distribution of X and Y is given by $f(x, y) = 4xye^{-(x^2+y^2)}$ ; $x \ge 0$ , $y \ge 0$   |                        |
| Find the marginal density functions of $X$ and $Y$ and test whether $X$ and $Y$ are independent, in a constant of $X$ and $Y$ are independent, in a constant of $X$ and $Y$ and $Y$ and $Y$ are independent, in a constant of $X$ and $Y$ and $Y$ and $Y$ are independent, in a constant of $X$ and $Y$ and $Y$ and $Y$ are independent, in a constant of $X$ and $Y$ and $Y$ and test whether $X$ and $Y$ are independent, in a constant of $X$ and $Y$ and $Y$ and test whether $X$ and $Y$ are independent, in a constant of $X$ and $Y$ and $Y$ and test whether $X$ and $Y$ are independent, in a constant of $X$ and $Y$ are independent, in a constant of $X$ and $Y$ are independent, in a constant of $X$ and $Y$ are independent, in a constant of $X$ and $Y$ are independent, in a constant of $X$ and $Y$ are independent, in a constant of $X$ and $Y$ are independent, in a constant of $X$ and $Y$ are independent, in a constant of $X$ and $Y$ are independent, in a constant of $X$ and $Y$ are independent, in a constant of $X$ and $Y$ and $Y$ and test whether $X$ and $Y$ are independent, in a constant of $X$ and $Y$ are independent, in a constant of $X$ and $Y$ are independent, in a constant of $X$ and $Y$ are independent, in a constant of $X$ and $Y$ are independent, in a constant of $X$ and $Y$ are independent, in a constant of $X$ and $X$ are included as $X$ and $X$ are include  | 3                      |
| 5.a) The following data pertain to the marks in subjects A and B in a certain examination Mean marks in A=39.5; Mean marks in B=47.5; Standard deviation of marks in A=10.8; Standard deviation of marks in B=16.8. Coefficient of correlation between marks in A and marks in B=0.42. Compute the two lines of regression and explain   | :<br>1                 |
| why there are two regression equations. Give the estimate of marks in Binform candidates who secured 50 marks in A.  b) Two independent variables are defined as   |                        |
| $f(x) = \begin{cases} 4ax & 0 \le x \le r \\ 0 & otherwise \end{cases}, \ f(y) = \begin{cases} 4by & 0 \le y \le s \\ 0 & otherwise \end{cases}. \ \text{If } U = X + Y \text{ and } V = X - Y \text{ and } V = X -$ |                        |
| then show that $Cov(U,V) = \frac{b-a}{b+a}$ .  | HAR HAR                |
| 6.a) Fit a Poisson distribution to the following data and test for the goodness of fit:  |                        |
| X: 0 1 2 3<br>Frequency: 24 15:::6: 5  |                        |
| b) Two independent samples of sizes 8 and 7 items respectively had the following values.   |                        |
| Sample I 11 11 13 11 15 9 12 14 Sample II 9 11 10 1 13 9 10 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1  | PÉ                     |
| Is the difference between the means of the sample significant? Test at 5% LOS. [5+5]   |                        |
| OR  7.a) Explain the concepts of confidence intervals and the standards error of an estimate.  | P6                     |
| Sample I 16 17 18 19 20 21 22 23 24  Sample II 12 17 18 22 27 23 32  Find the variances of the two samples and test whether the two populations have the same variance at 5% level of significance.  [5+5]   | PS.                    |
| P6 P6 P6 P6 P6   | FS                     |

| ·bic  | otain the steady<br>bbability that atle<br>eue length.                         | state solution<br>east one unit is j | present in the sy   | (M/M/1):(∞/Forstern and also fi | CFS). Find the nd the expected [10] | F.S. |  |  |  |
|---|--|--------------------------------------|---------------------|---------------------------------|-------------------------------------|------|--|--|--|
| OR  9. Define pure birth-death processes. Cars arrive at a pollution testing center according to Poisson distribution at an average rate of 15 cars per hour. The testing center can accommodate at maximum: 15 cars. The service time per car is an exponential distribution with mean rate 10 per hour. (a) What is the probability that an arriving car does not have to wait for testing. (b) What is the expected waiting time until a car is left from the testing center.  [5+5] |  |                                      |                     |                                 |                                     |      |  |  |  |
| b) Des  | ine Markov process.  cribe stationary a  ine stochastic pro rix said to be reg | and non-stationar                    | y random proces  OR | s.                              | [5+5]                               | P6   |  |  |  |
|   | ve that: the mat   |                                      | is the transi       | tion probability                | matrix of an                        | F'6  |  |  |  |
| irred   | lucible Markov c   | hain.                                | -                   |                                 | [5+5]                               |      |  |  |  |
| P£  | P6   |                                      | 0000                | P6                              | PS                                  | Fi   |  |  |  |
| PS  | P6,  | PE                                   | FÉ                  | P6                              | P6                                  | Pé   |  |  |  |
| PS  | PĠ   | FE                                   | PE                  | P6                              | P6                                  | PE   |  |  |  |
| P6  | PS   | F6                                   | P6                  | F6                              | P6                                  | P6   |  |  |  |
| FE  | P6   | F.S                                  | FE                  | PE                              | P6                                  | PS   |  |  |  |

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