

**R18**

Code No: 153BT

**JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD**

**B. Tech II Year I Semester Examinations, December - 2019**

**SIGNALS AND SYSTEMS**  
(Common to ECE, EIE)

Time: 3 Hours

Max. Marks: 75

**Note:** This question paper contains two parts A and B.

Part A is compulsory which carries 25 marks. Answer all questions in Part A. Part B consists of 5 Units. Answer any one full question from each unit. Each question carries 10 marks and may have a, b as sub questions.

**PART - A**

(25 Marks)

- 1.a) List out the properties of an impulse function. [2]
- b) State the Dirichlets conditions for convergence of Fourier series [2]
- c) State the Paley-Wiener criterion for physical realizability of the system. [2]
- d) Find the Laplace Transform of the signal  $x(t) = \sin(t) + \cos(t)$  [2]
- e) What is meant by Aliasing? [2]
- f) What is complete set of orthogonal functions? [3]
- g) Find and Sketch the Fourier Spectrum of the signal  $x(t) = \frac{1}{t}$  [3]
- h) Find and Sketch the conditions for distortion less transmission System. [3]
- i) Find the Z-Transform of the sequence  $x(n) = a^n u(n) - (b)^n u(-n-1)$  [3]
- j) Determine the Autocorrelation Function of a signal  $x(t) = e^{-at} u(t)$  [3]

**PART - B**

(50 Marks)

- 2.a) Define signal space. Give an example of a signal space, and also define the term 'basis set' for a signal space.
- b) Find the even and odd components of an unit step signal, and also show that these components are orthogonal functions. [5+5]

**OR**

- 3.a) If  $x(t) = \begin{cases} 1-|t|; & -1 \leq t \leq 1 \\ 0 & \text{otherwise} \end{cases}$ ; then sketch the signal  $x\left(\frac{-t+1}{2}\right) + x\left(\frac{-t-1}{2}\right)$

- b) How to approximate a function by set of mutually orthogonal functions. Derive the necessary equations. [5+5]

- 4.a) Find the TFS of an even symmetric square wave periodic signal with period  $T_0$ .

- b) Find the TFS of a Quarter wave odd symmetric periodic signal. [5+5]

**OR**

- 5.a) If  $x(t)$  and  $X(\omega)$  forms the Fourier Transform pair, then find the Inverse Fourier

Transform of: i)  $X(\omega) = \frac{1}{1+\omega^2}$  ii)  $X(\omega) = \text{sgn}(\omega)$

- b)  $x(t)$  and  $X(\omega)$  forms the Fourier Transform pair, prove that, if  $x(t)$  is real and even, then  $X(\omega)$  is also real and even. [5+5]



6. The continuous -time LTI system is described by the following differential equation

$$y'(t) + 2y(t) = x(t)$$

a) Verify that the impulse response of this system is  $h(t) = e^{-2t}u(t)$

b) Is this system i) Memoryless ii) Causal iii) Stable. Justify your answer. [5+5]

OR

7.a) Find the necessary and sufficient condition on the impulse response  $h(t)$  such that system is BIBO Stable.

b) Find and sketch the impulse response of an Ideal BPF. [5+5]

8.a) Determine the Laplace Transform, also sketch the pole, zero locations, and associated ROC of the signal  $x(t) = -e^{-at}u(-t)$ ,  $a < 0$ .

b) The input and output relationship of the continuous time system is

$$y''(t) - y'(t) - 2y(t) = x(t)$$

Determine the step response of the system when the system is causal. [5+5]

OR

9.a) State and prove Final value Theorem of Z-Transform.

b) If  $h(n)$  and  $H(Z)$  forms Z-Transform pair, then find the Inverse Z-Transform of  $Z^{-N}H(-Z^{-1})$ . [5+5]

10.a) Derive Relation between correlation and convolution.

b) Find the convolution of the following signal by graphical method

$$x(t) = e^{-3t}u(t), h(t) = u(t+3)$$

[5+5]

OR

11.a) Determine the output of the system for the input  $x(t)$  and the impulse response of the

$$\text{system is } h(t), \text{ where } x(t) = \begin{cases} 1; & -0.5 \leq t \leq 0.5 \\ 0; & \text{otherwise} \end{cases} \text{ and } h(t) = \begin{cases} 1; & 0 \leq t \leq 1 \\ 0; & \text{otherwise} \end{cases}$$

b) Derive the relationship between Autocorrelation Function and Power Spectral density. [5+5]

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