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Code No: 431AA

R16

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD

B.Tech I Year I Semester Examinations, May/June - 2017

MATHEMATICS-I

(Common to CE, EEE, ME, ECE, CSE, EIE, IT, MCT, MMT, MIE, CEE, MSNT)

Time: 3 hours

Max. Marks: 75

Note: This question paper contains two parts A and B.

Part A is compulsory which carries 25 marks. Answer all questions in Part A.

Part B consists of 5 Units. Answer any one full question from each unit. Each question carries 10 marks and may have a, b, c as sub questions.

Part- A (25 Marks)

1.a) Verify  $y(2x^2 - xy + 1)dx + (x - y)dy = 0$  is an exact differential equation or not? [2]

b) Solve  $y'' + 6y' + 9y = 0, y(0) = 2, y'(0) = -3$  [3]

c) Find the rank of the matrix  $A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 3 & 1 & 2 \end{bmatrix}$  [2]

d) Find a non trivial solution of homogeneous system  $3x + 2y + z = 0, 2x + 3z = 0, y + 5z = 0$ , if it exist. [3]

e) Find all the Eigen values of  $A^2 + 3A - 2I$ , if  $A = \begin{bmatrix} 1 & 2 \\ 1 & 0 \end{bmatrix}$ . [2]

f) Find the nature, index and signature of the quadratic form  $3x^2 + 5y^2 + 3z^2$ . [3]

g) State Euler's theorem for function of two variables. [2]

h) Examine the function  $f(x, y) = x^3 y^2$  for extrema. [3]

i) Solve  $(p-q)(z-px-qy)=1$  [2]

j) Solve  $xp + yq = 3z$  [3]

Part-B (50 Marks)

2.a) Solve  $(x^2 y - 2xy^2)dx - (x^3 - 3x^2 y)dy = 0$

b) Find the orthogonal trajectories of the family of Cardioids  $r = a(1 - \cos\theta)$ , where  $a$  is the parameter. [5+5]

OR

3.a) Solve  $y'' - 2y' + y = xe^x \sin x$

b) The number  $N$  of bacteria in a culture grew at a rate proportional to  $N$ . The value of  $N$  was initially 100 and increased to 332 in one hour. What would be the value of  $N$  after  $1 \frac{1}{2}$  hours? [5+5]

4.a) Determine the value of  $b$  such that the rank of  $A = \begin{bmatrix} 1 & 1 & -1 & 0 \\ 4 & 4 & -3 & 1 \\ b & 2 & 2 & 2 \\ 9 & 9 & b & 3 \end{bmatrix}$  is 3.

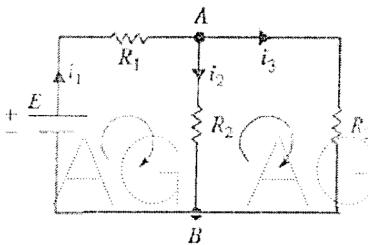
b) Discuss for what values of  $\lambda$  and  $\mu$ , the simultaneous equations  $x + y + z = 6$ ,  $x + 2y + 3z = 10$ ,  $x + 2y + \lambda z = \mu$  have i) no solution ii) a unique solution iii) an infinite number of solutions. [5+5]

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5.a) Find the rank of the matrix  $A = \begin{bmatrix} 2 & 1 & 3 & 5 \\ 4 & 2 & 1 & 3 \\ 8 & 4 & 7 & 13 \end{bmatrix}$

$$\begin{array}{r} \\ \\ \\ \end{array} \left[ \begin{array}{cccc} 2 & 1 & 3 & 5 \\ 4 & 2 & 1 & 3 \\ 8 & 4 & 7 & 13 \end{array} \right]$$

b) Use Gauss Jordan elimination method to solve the following network system, when  $R_1=10$  ohms,  $R_2=20$  ohms,  $R_3=10$  ohms and  $E=12$  volts. [5+5]



6.a) Find the Eigen values and the corresponding Eigen vectors of the matrix

$$A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$$

b) Verify Cayley-Hamilton theorem for the matrix  $A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 5 \\ 3 & 5 & 6 \end{bmatrix}$ . Express

$B = A^8 - 11A^7 - 4A^6 + A^5 + A^4 - 11A^3 - 3A^2 + 2A + I$  as a quadratic polynomial in  $A$ .  
Find  $B$ . [5+5]

7.a) Diagonalize the matrix  $A = \begin{bmatrix} 1 & 1 & 1 \\ 0 & 2 & 1 \\ -4 & 4 & 3 \end{bmatrix}$ , hence find  $A^4$ .

b) Reduce the quadratic form  $x^2 + y^2 + 2z^2 - 2xy + 4xz + 4yz$  to the canonical form. Hence find its nature. [5+5]

8.a) If  $u = \log\left(\frac{x^2 + y^2}{x + y}\right)$ , prove that  $xu_x + yu_y = 1$

b) If  $u = x^2 - y^2$ ,  $v = 2xy$  when  $x = r\cos\theta$ ,  $y = r\sin\theta$ . Show that  $\frac{\partial(u, v)}{\partial(r, \theta)} = 4r^3$ . [5+5]

9.a) Expand  $f(x, y) = e^y \ln(1+x)$  in powers of  $x$  and  $y$  and verify the result by direct expansion.

b) Find the extreme values of  $\sqrt{x^2 + y^2}$  when  $13x^2 + 13y^2 - 10xy = 72$ . [5+5]

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10.a) Form the partial differential equation from  $z = x^n f\left(\frac{y}{x}\right)$ .

AG AG AG AG OR AG AG AG [5+5]

11.a) Solve  $(z-y)p + (x-z)q = y-x$ .

b) Solve  $z^2(p^2x^2 + q^2) = 1$ .

[5+5]

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