Code No: 133BD

R16

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD
B.Tech II Year I Semester Examinations, November/December - 2017
MATHEMATICS – IV
(Common to CE, EEE, ME, ECE, CSE, EIE, IT, MCT, MMT, AE, MIE, PTM, CEE, MSNT)
Time: 3 Hours
Max. Marks: 75

Note: This question paper contains two parts A and B.
Part A is compulsory which carries 25 marks. Answer all questions in Part A.
Part B consists of 5 Units. Answer any one full question from each unit.
Each question carries 10 marks and may have a, b, c as sub-questions.

PART- A

(25 Marks)

1.a) Show that $f(z) = z + \bar{z}$ is not analytic any where in the complex plane. [2]

b) Write Cauchy-Remainn equations in Polar form. [3]

c) Find the residues at the poles of the function $f(z) = \dfrac{1}{(z+1)(z+2)}$. [2]

d) Expand $f(z) = Tanz$ in Taylor's series about the point $z=0$. [3]

e) Define Bilinear transformation. [2]

f) Define for a complex function: i) Isolated Singularity ii) Removable Singularity. [3]

g) If $f(x) = x^2$ in $[-\pi, \pi]$, find a_0 in Fourier series. [2]

h) State Fourier integral theorem. [3]

i) Write the one dimensional Heat equation in steady state. [2]

j) Classify partial differential equation $\dfrac{\partial^2 z}{\partial x^2} - 2\dfrac{\partial z}{\partial x} + \dfrac{\partial z}{\partial y} = 0$. [3]

PART-B

(50Marks)

2.a) Determine p so that the function $f(z) = \frac{1}{2}\log(x^2 + y^2) + Tan^{-1}(\frac{px}{y})$ is analytic.

b) Find the analytic function $f(z) = u + iv$ if $u - v = e^x[\cos y - \sin y]$. [5+5]

OR

3.a) Determine the analytical function whose real part is $x^3 - 3xy^2 + 3x^2 - 3y^2 = 1$. Also find the harmonic conjugate of this real part.

b) Prove that $\left[\dfrac{\partial^2}{\partial x^2} + \dfrac{\partial^2}{\partial y^2}\right]|f(z)|^2 = 4|f'(z)|^2$. [5+5]

4.a) Using Cauchy integral formula, find $\int_c \dfrac{e^{2z}}{(z+1)^3} dz$, where C is the curve $|z| = 2$.

b) Evaluate $\int (x^2 - iy^2)dz$ along a straight line from $(0,0)$ to $(0,1)$ and then from $(0,1)$ to $(2,1)$. [5+5]

OR

5. Find Laurent's series of $\dfrac{z}{(z-1)(z-2)}$ about:

a) $|z| < 1$ b) $|z| > 1$ c) $1 < |z| < 2$ [10]

6. Evaluate $\int_0^{2\pi} \frac{\cos 3\theta}{5-4\cos\theta}\, d\theta$. [10]

OR

7. Find Mobius transformation that maps:
   a) $0, 1, \infty$ into $-5, -1, 3$, Find fixed points.
   b) $\infty, i, 0$ to $0, -i, \infty$. [5+5]

8. Find the Fourier series of $f(x) = e^{-x}$ in the interval(0.2π). Hence, deduce that
   $$\frac{\pi}{2}\frac{1}{\sin h\pi} = \sum_{n=2}^{\infty} \frac{(-1)^n}{n^2+1}$$ [10]

OR

9.a) Find the Fourier series for $f(x) = x + x^2$ in $-\pi < x < \pi$.

   b) Find the Fourier cosine transform of e^{-x^2} [5+5]

10. Solve $\frac{\partial u}{\partial x} = 4\frac{\partial u}{\partial y}$, $u(0, y) = 8e^{-3y}$ by the method of separation of variables. [10]

OR

11. The ends of a uniform string of length $2l$ are fixed. The initial displacement is m $y(x. 0) = 3x(2l - x), 0 < x < 2l$, while the initial velocity is zero, Find the displacement at any distance x from the end $x=0$ at any time 't'. [10]

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