

**Answer any five questions
All questions carry equal marks**

- 1.a) Find the impulse response $h[n]$ of the system described by the difference equation

$$8y[n] + 6y[n-1] = x[n]$$
- b) Discuss the sampling rate conversion by a factor 1 with the help of a neat block diagram.
- c) Define time invariant system. Show that the interpolator is a time-variant system. [5+5+5]
- 2.a) Check the following filter for time invariant, causal and linear.
 (i) $y(n) = (n-1)x^2(n+1)$ (ii) $y(n) = n^2x(n-2)$
- b) Explain the frequency domain representation of discrete time signals.
- c) Explain the terms: i) Up – sampling ii) Down- sampling. [5+5+5]
- 3.a) Determine the Inverse Z-Transform of $X(Z) = \frac{1}{(1-Z^{-1})(1-Z^{-1})^2}$
- b) Find the linear convolution of the sequences $x[n] = \{1,4,0,9, -1\}$ and $h[n] = \{-3, -4,0,7\}$.
- c) Compute the DFT of the sequence $x(n) = \sin[n\pi/4]$, where $N=8$ using DIT FFT algorithm. [5+5+5]
- 4.a) Write five properties of DFS.
- b) Find the Laplace transform of the following function $f(t) = te^{2t} \sin(3t)$.
- c) Given $x(n) = \{1,2,3,4,4,3,2,1\}$, find $X(k)$ using DIF FFT algorithm. [5+5+5]
- 5.a) Design a Chebyshev filter with a maximum passband attenuation of 2 dB; at $\Omega_p=20$ rad/sec and the stopband attenuation of 35 dB at $\Omega_s=50$ rad/sec.
- b) Obtain the impulse response of digital filter to correspond to an analog filter with impulse response $h_a(t) = 0.5 e^{-2t}$ and with a sampling rate of 1.0kHz using impulse invariant method. [7+8]
- 6.a) Differentiate "maximally flat magnitude response" and "equiripple magnitude response" filters.
- b) Convert the analog filter to a digital filter whose system function is $H(S) = \frac{1}{(S+2)^2(S+1)}$. Use bilinear transformation. [8+7]
- 7.a) What is a Kaiser window? In what way is it superior to other window functions?
- b) Using a rectangular window technique, design a low pass filter with pass band gain of unity, cut-off frequency of 1000Hz and working at a sampling frequency of 5 KHz. The length of the impulse response should be 7. [7+8]
- 8.a) Using the z-transform, find the total solution to the following difference equation with initial conditions, for discrete time $n \geq 0$,

$$5y[n+2] - 3y[n+1] + y[n] = (0.8)^n u[n], y[0] = -1, y[1] = 10$$
- b) Determine direct form I and cascade realization of the following system: [8+7]

$$H(z) = \frac{2(1-z^{-1})(1+\sqrt{2}z^{-1}+z^{-2})}{(1+0.5z^{-1})(1-0.9z^{-1}+0.81z^{-2})}$$